

SECONDARY MATHEMATICS III—HONORS STANDARDS

Strand: NUMBER AND QUANTITY—Complex Number System (N.CN)

Perform arithmetic operations with complex numbers (**Standard N.CN.3**). Represent complex numbers and their operations on the complex plane (**Standard N.CN.4–6**). Use complex numbers in polynomial identities and equations (**Standard N.CN.10**).

- **Standard N.CN.3** Find the conjugate of a complex number; use conjugates to find moduli and quotients of complex numbers.
- **Standard N.CN.4** Represent complex numbers on the complex plane in rectangular form and polar form (including real and imaginary numbers), and explain why the rectangular form of a given complex number represents the same number.
- **Standard N.CN.5** Represent addition, subtraction, multiplication, and conjugation of complex numbers geometrically on the complex plane; use properties of this representation for computation. *For example, $(-1 + \sqrt{3}i)^3 = 8$ because $(-1 + \sqrt{3}i)$ has modulus 2 and argument 120° .*
- **Standard N.CN.6** Calculate the distance between numbers in the complex plane as the modulus of the difference, and the midpoint of a segment as the average of the numbers at its endpoints.
- **Standard N.CN.10** Multiply complex numbers in polar form and use DeMoivre’s Theorem to find roots of complex numbers.

Strand: FUNCTIONS—Interpreting Functions (F.IF)

Analyze functions using different representations (**Standard F.IF.7, d and f**).

- **Standard F.IF.7** Graph functions expressed symbolically, and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
 - d. Graph rational functions, identifying zeros, asymptotes, and point discontinuities when suitable factorizations are available, and showing end behavior.
 - f. Define a curve parametrically and draw its graph.

Strand: FUNCTIONS—Building Functions (F.BF).

Build a function that models a relationship between two quantities (**Standard F.BF.1.c**). Build new functions from existing functions (**Standards F.BF.4, b,c,d–5**).

- **Standard F.BF.1** Write a function that describes a relationship between two quantities.
 - c. Compose functions. *For example, if $T(y)$ is the temperature in the atmosphere as a function of height, and $h(t)$ is the height of a weather balloon as a function of time, then $T(h(t))$ is the temperature at the location of the weather balloon as a function of time.*

- **Standard F.BF.4** Find inverse functions.
 - b. Verify by composition that one function is the inverse of another.
 - c. Read values of an inverse function from a graph or a table, given that the function has an inverse.
 - d. Produce an invertible function from a non-invertible function by restricting the domain.
- **Standard F.BF.5** Understand the inverse relationship between exponents and logarithms, and use this relationship to solve problems involving logarithms and exponents.

Strand: FUNCTIONS—Trigonometric Functions (F.TF)

Extend the domain of trigonometric functions using the unit circle (**Standard T.FT.4**). Model periodic phenomena with trigonometric functions (**Standards T.FT.6–7**). Prove and apply trigonometric identities (**Standard T.FT.9**).

- **Standard F.TF.4** Use the unit circle to explain symmetry (odd and even) and periodicity of trigonometric functions.
- **Standard F.TF.6** Understand that restricting a trigonometric function to a domain on which it is always increasing or always decreasing allows its inverse to be constructed.
- **Standard F.TF.7** Use the inverse functions to solve trigonometric equations that arise in the modeling contexts; evaluate the solutions using technology, and interpret them in terms of the context.
- **Standard F.TF.9** Prove the addition and subtraction formulas for sine, cosine, and tangent, and use them to solve problems.

Strand: GEOMETRY—Geometric Measurement and Dimension (G.GMD)

Explain volume formulas and use them to solve problems (**Standard G.GMD.2**).

- **Standard G.GMD.2** Give an informal argument using Cavalieri's principle for the formulas for the volume of a sphere and other solid figures.

Strand: STATISTICS AND PROBABILITY—Conditional Probability and the Rules of Probability (S.CP)

Use the rules of probability to compute probabilities of compound events in a uniform probability model (**Standard S.CP.9**).

- **Standard S.CP.9** Use permutations and combinations to compute probabilities of compound events and solve problems.